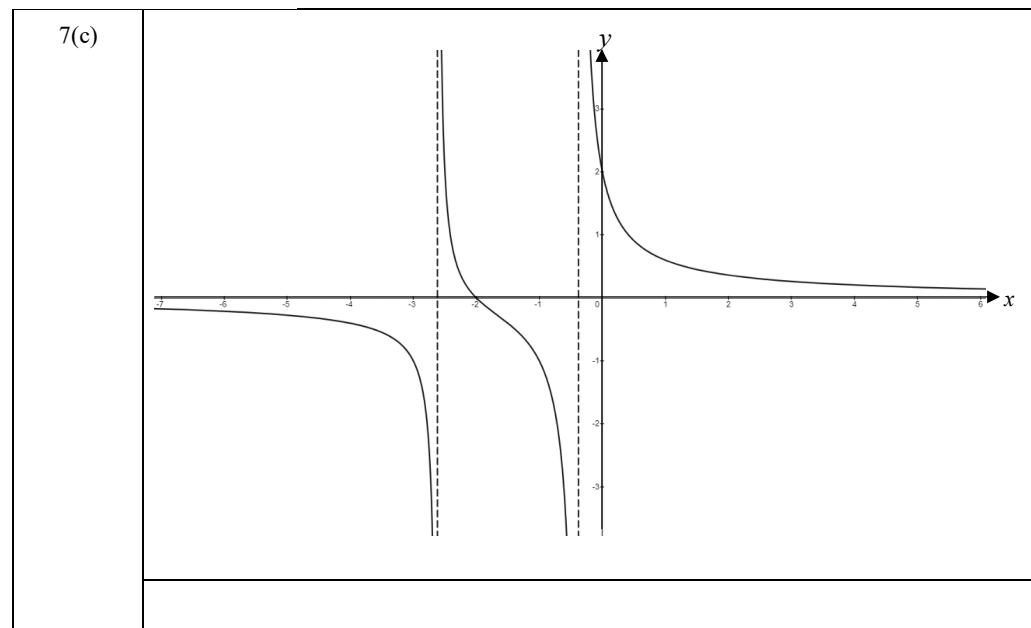
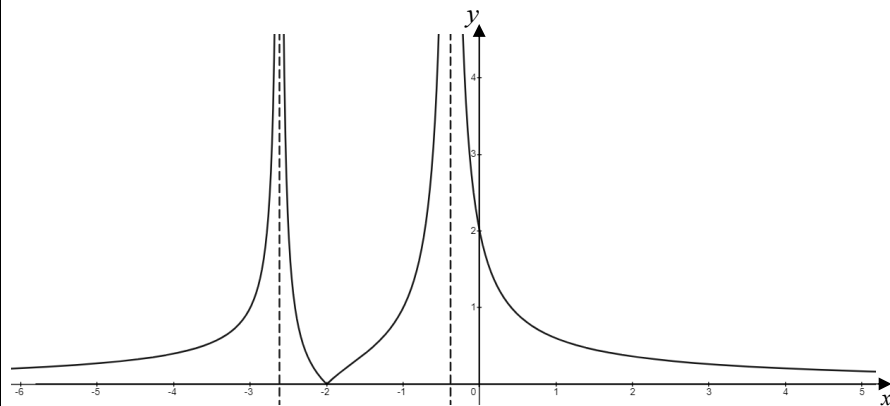


7(a)	$x = -\frac{3}{2} - \frac{1}{2}\sqrt{5}, \quad x = -\frac{3}{2} + \frac{1}{2}\sqrt{5}$
	$y = 0$
7(b)	$\frac{dy}{dx} = \frac{(x^2 + 3x + 1)(1) - (x + 2)(2x + 3)}{(x^2 + 3x + 1)^2}$
	$x^2 + 4x + 5 = 0$
	Discriminant is $4^2 - 20 = -4 < 0$ so no real roots.



7(d)



7(e)

$$\frac{x+2}{x^2+3x+1} = 2 \text{ or } \frac{x+2}{x^2+3x+1} = -2$$

$$-2x^2 - 5x = 0 \text{ or } 2x^2 + 7x + 4 = 0$$

$$x = -\frac{5}{2}, \quad x = 0 \text{ or } x = -\frac{7}{4} - \frac{1}{4}\sqrt{17}, \quad x = -\frac{7}{4} + \frac{1}{4}\sqrt{17}$$

$$-\frac{7}{4} - \frac{1}{4}\sqrt{17} < x < -\frac{5}{2}, \quad -\frac{7}{4} + \frac{1}{4}\sqrt{17} < x < 0, \quad x \neq -\frac{3}{2} \pm \frac{1}{2}\sqrt{5}$$

7(a)

$$x = -1$$

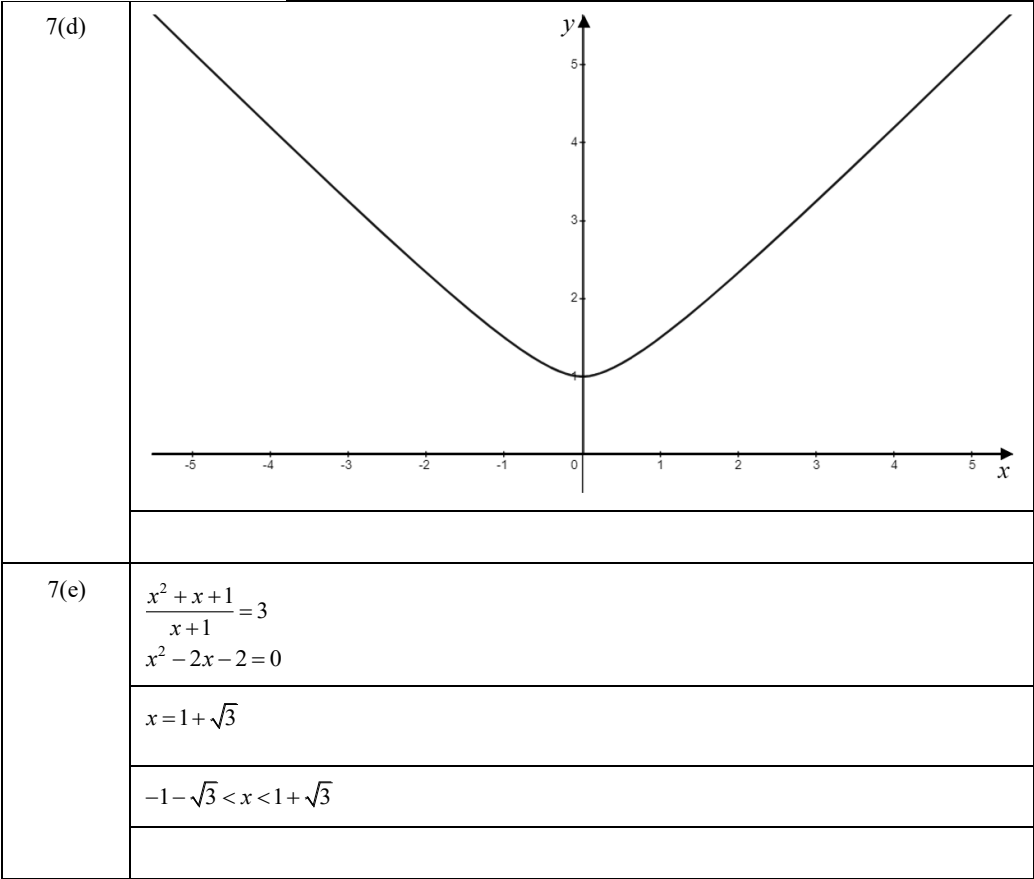
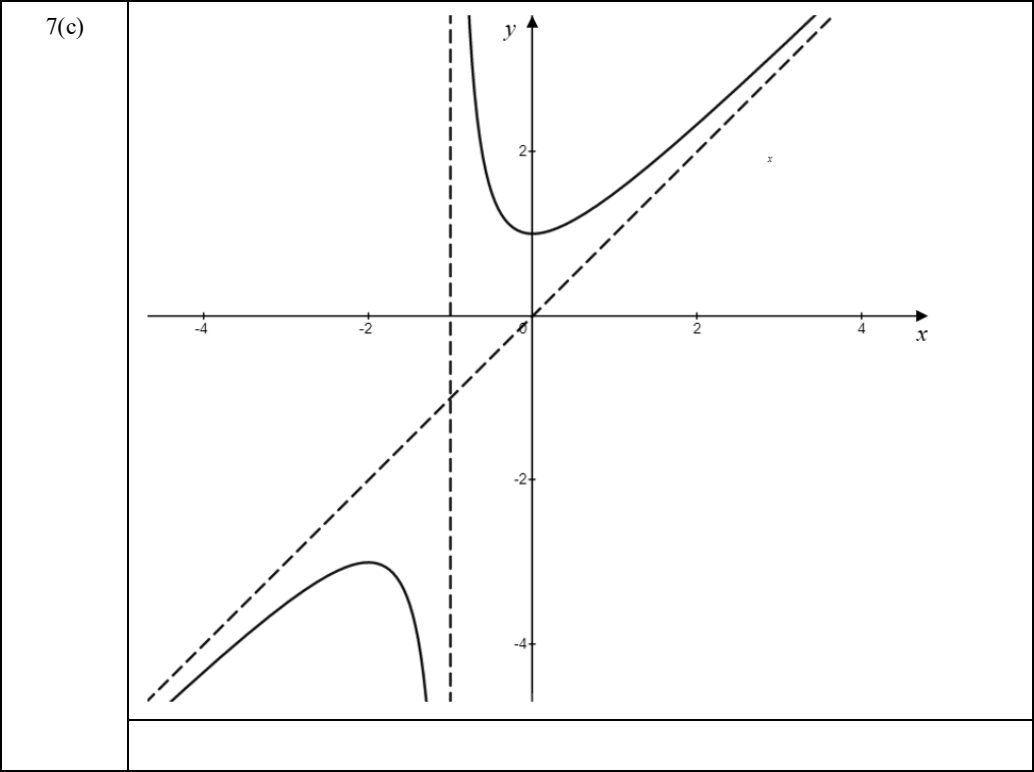
$$y = \frac{x(x+1)+1}{x+1}$$

$$y = x$$

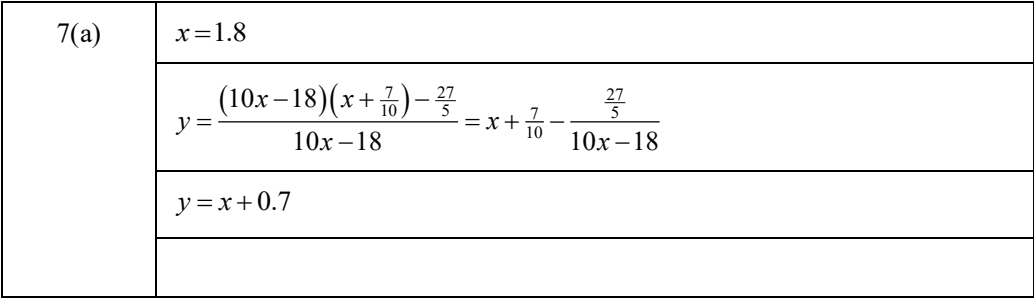
7(b)

$$\frac{dy}{dx} = \frac{x^2+2x}{(x+1)^2} = 0$$

$$(0,1), \quad (-2,-3)$$



7(e)

$$\frac{x^2 + x + 1}{x + 1} = 3$$
$$x^2 - 2x - 2 = 0$$
$$x = 1 + \sqrt{3}$$
$$-1 - \sqrt{3} < x < 1 + \sqrt{3}$$


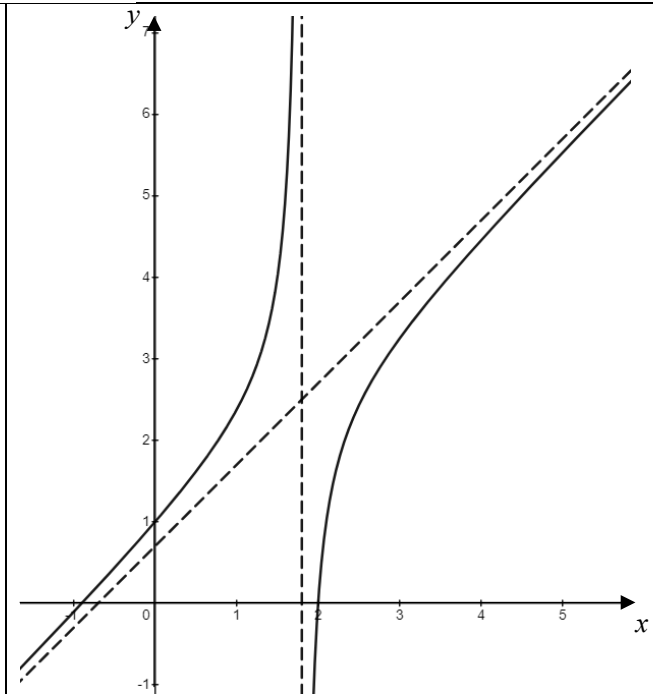
7(b)

$$\frac{dy}{dx} = \frac{100x^2 - 360x + 378}{(10x - 18)^2}$$

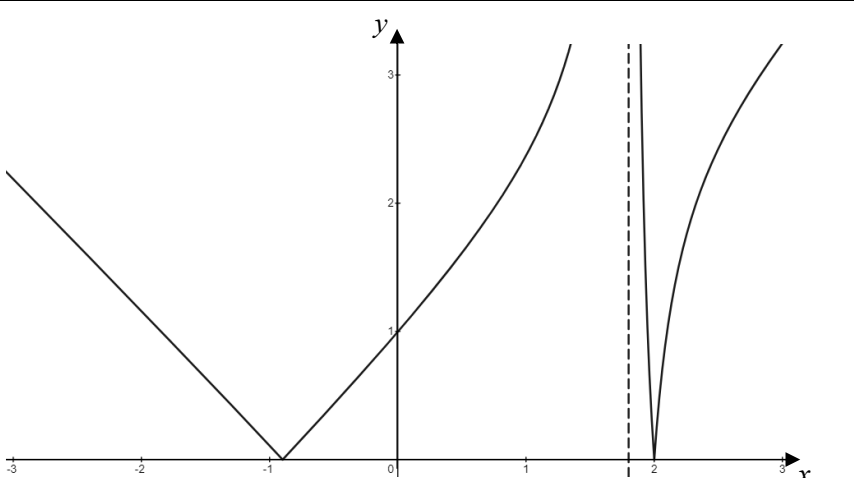
$$50x^2 - 180x + 189 = 0 \quad \left(\text{or } \frac{dy}{dx} = 1 + \frac{54}{(10x - 18)^2} \right)$$

$$180^2 - 4(50)(189) = -5400 < 0 \quad (\text{or } y' > 0) \Rightarrow \text{No stationary points}$$

7(c)

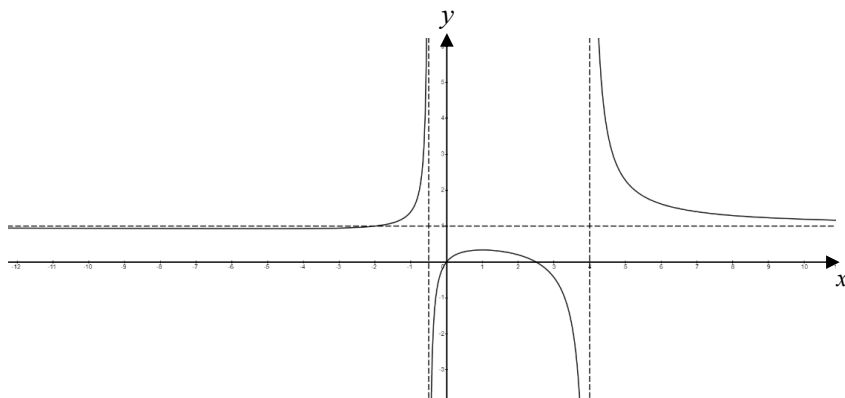


(0,1), (-0.9,0), (2,0)

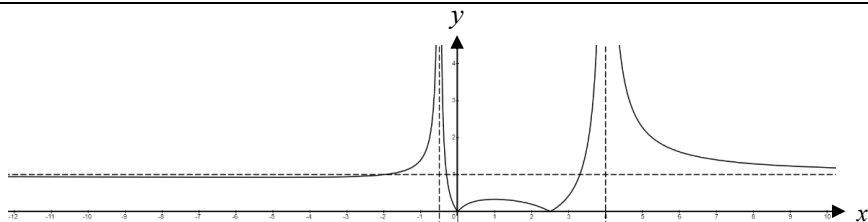
7(d)	
7(e)	$\left[\frac{10x^2 - 11x - 18}{10x - 18} = -4 \Rightarrow x = \frac{-29 \pm \sqrt{4441}}{20} \right]$
	$\frac{10x^2 - 11x - 18}{10x - 18} = 4$
	$10x^2 - 51x + 54 = 0$
	$p = \frac{3}{2}, \quad q = \frac{18}{5}$

7(a)	$x = -\frac{1}{2}, \quad x = 4$
	$y = 1$
7(b)	$\frac{dy}{dx} = \frac{(2x^2 - 7x - 4)(4x - 5) - (2x^2 - 5x)(4x - 7)}{(2x^2 - 7x - 4)^2}$
	$4x^2 + 16x - 20 = 0$
	$\left(-5, \frac{25}{27}\right) \quad \left(1, \frac{1}{3}\right)$

7(c)

 $(0,0), \left(\frac{5}{2}, 0\right)$

7(d)



7(e)

$$\frac{2x^2 - 5x}{2x^2 - 7x - 4} = \frac{1}{9} \text{ or } \frac{2x^2 - 5x}{2x^2 - 7x - 4} = -\frac{1}{9}$$

$$16x^2 - 38x + 4 = 0 \text{ or } 20x^2 - 52x - 4 = 0$$

$$x = \frac{19}{16} + \frac{3}{16}\sqrt{33}, \quad x = \frac{19}{16} - \frac{3}{16}\sqrt{33} \text{ or } x = \frac{13}{10} + \frac{3}{10}\sqrt{21}, \quad x = \frac{13}{10} - \frac{3}{10}\sqrt{21}$$

$$\frac{13}{10} - \frac{3}{10}\sqrt{21} < x < \frac{19}{16} - \frac{3}{16}\sqrt{33}, \quad \frac{19}{16} + \frac{3}{16}\sqrt{33} < x < \frac{13}{10} + \frac{3}{10}\sqrt{21}$$

6(a)

$$x = -a$$

$$y = \frac{(x+a)(x-a) + a^2 + a}{x+a} = x - a + \frac{a^2 + a}{x+a}$$

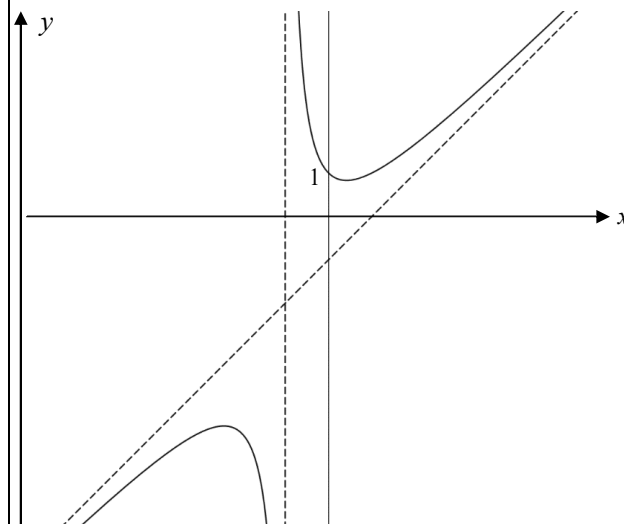
$$y = x - a$$

6(b)

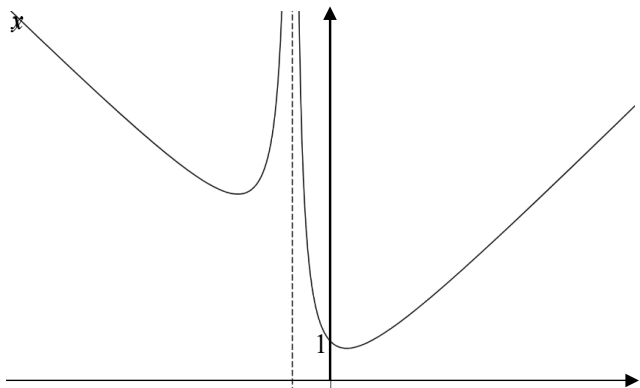
$$\frac{dy}{dx} = 1 - (a^2 + a)(x+a)^{-2} = 0 \text{ or } x^2 + 2ax - a = 0$$

$$x = -a \pm \sqrt{a^2 + a}$$

6(c)



6(d)



6(e)

$$\frac{x^2 + a}{x + a} = a$$

$$x^2 - ax + a - a^2 = 0$$

$$\text{Or } \frac{x^2 + a}{x + a} = -a \Rightarrow x^2 + ax + a + a^2 = 0$$

$$a^2 - 4(a - a^2) = 5a^2 - 4a > 0$$

$$a > \frac{4}{5}.$$