

4(a)	$G_X(t) = \frac{2}{5}t + \frac{3}{5}t^2$
4(b)	$G_Y(t) = \frac{1}{625}t^4(2+3t)^4 \quad \left[= t^4 \left(\frac{2}{5} + \frac{3}{5}t \right)^4 \right]$
4(c)	Attempt at coefficient of t^6 in <i>their</i> $G_Y(t)$.
	$P(Y = 6) = \frac{216}{625}$

4(d)

$$G_Y'(t) = \frac{4}{625}t^3(2+3t)^4 + \frac{12}{625}t^4(2+3t)^3$$

$$\text{OR } G_Y'(t) = \frac{1}{625}(64t^3 + 480t^4 + 1296t^5 + 1512t^6 + 648t^7)$$

$$G_Y''(t) = \frac{12}{625}t^2(2+3t)^4 + \frac{96}{625}t^3(2+3t)^3 + \frac{108}{625}t^4(2+3t)^2$$

$$\text{OR } G_Y''(t) = \frac{1}{625}(192t^2 + 1920t^3 + 6480t^4 + 9072t^5 + 4536t^6)$$

$$G_Y'(1) = \frac{32}{5} = 6.4, \quad G_Y''(1) = \frac{888}{25} = 35.52$$

$$\text{Var}(Y) = \frac{888}{25} + \frac{32}{5} - \left(\frac{32}{5}\right)^2$$

$$\text{Var}(Y) = \frac{24}{25} \quad [= 0.96]$$

Alternative method for question 4(d)

$$E(X) = \frac{2}{5} + \frac{3}{5} \times 2 = \frac{8}{5} \text{ or use } G_X'(t) = \frac{2}{5} + \frac{6}{5}t.$$

$$E(X^2) = \frac{2}{5} + \frac{3}{5} \times 4 = \frac{14}{5} \text{ or use } G_X''(t) = \frac{6}{5}$$

$$\text{Var}(X) = \frac{14}{5} - \left(\frac{8}{5}\right)^2 \text{ or } \text{Var}(X) = \frac{6}{5} + \frac{8}{5} - \left(\frac{8}{5}\right)^2$$

$$\text{Var}(X) = \frac{6}{25}$$

$$\text{Var}(Y) = 4\text{Var}(X) = \frac{24}{25}$$