

1.4 Matrices

Name: _____ Class: _____ Date: _____

Total: 13 marks

KEY WORDS transformations 变换 • rotation 旋转 • inverse 逆矩阵 • enlargement 放大
• determinant 行列式

Objective

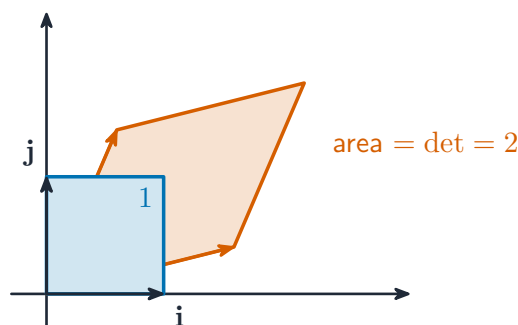
Build the skills to answer exam questions on **matrices** 矩阵 — multiplication, the **determinant** 行列式 and **inverse** 逆矩阵, and 2×2 matrices as **transformations** 变换.

You must be able to:

- multiply matrices and use I
- find $\det A$ and A^{-1} for a 2×2 matrix; use $(AB)^{-1} = B^{-1}A^{-1}$
- identify the transformation a matrix represents (and its area scale factor)

1 Worked examples

■ Inverse & transformation



A matrix maps the unit square to a parallelogram whose area equals $\det A$

$$A = \begin{pmatrix} 3 & 1 \\ 2 & 4 \end{pmatrix}; \det A = 12 - 2 = 10; A^{-1} = \frac{1}{10} \begin{pmatrix} 4 & -1 \\ -2 & 3 \end{pmatrix}.$$

Transformations: $\begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$ is a 90° rotation; $\det = 1$ (area preserved).

2 Practice

2.1 Find $\det \begin{pmatrix} 5 & 2 \\ 3 & 4 \end{pmatrix}$. [1]

2.2 Find the inverse of $\begin{pmatrix} 2 & 1 \\ 1 & 1 \end{pmatrix}$. [2]

3 Exam-style questions

3.1 The matrix $\begin{pmatrix} 2 & 0 \\ 0 & 2 \end{pmatrix}$ represents: [1]

A	B
C	D

A a rotation

B an enlargement, scale factor 2

C a reflection

D a shear

3.2 $A = \begin{pmatrix} 1 & 2 \\ 3 & 4 \end{pmatrix}$ and $B = \begin{pmatrix} 2 & 0 \\ 1 & 3 \end{pmatrix}$.

(a) Find AB . [2]

(b) Find $\det(AB)$ and verify it equals $\det A \times \det B$. [3]

3.3 The transformation T has matrix $M = \begin{pmatrix} 3 & 1 \\ 0 & 2 \end{pmatrix}$.

(a) Find the area scale factor of T . [1]

(b) Find M^{-1} and hence the image-to-object matrix that undoes T . [3]
