

Data Representation

A-Level Computer Science

User-defined data types

The built-in types (INTEGER, REAL, STRING, CHAR, BOOLEAN) cover the simplest cases. For richer problems you can define **user-defined types** 用户定义类型, making the code clearer and the compiler stricter.

Why they are needed

A built-in STRING lets you store nonsense in a field that should hold one of a few legal values; a user-defined type can restrict it. Real entities are usually a **collection** of values of different types. And `DECLARE Taxi : Vehicle` is clearer (self-documenting) than `DECLARE Taxi : STRING`.

“Describe the purpose of a user-defined data type” (two marks). *A data type defined by the programmer, built from existing (built-in) types, so that data specific to the problem can be represented when no built-in type fits.* Both halves score: **defined by the programmer** and **based on existing types**. The examiner also accepts “to make the program easier to read and maintain” as a supporting point, never on its own.

“Explain what is meant by non-composite and composite data types” (four marks). A **non-composite** type is defined **without reference to another type**: it holds a **single** value, for example an integer, a real, or an enumerated value. A **composite** type is a collection of **other types** (which may themselves be composite): it holds **several** values under one identifier, for example a record, a set, an array or a class. Give an example with each definition; the exam asks for one.

Non-composite types

Enumerated type

An **enumerated type** 枚举类型 has values that are a **fixed list of named constants**:

```
TYPE Vehicle = (M100, M230, T101, T102, T120, T150)
DECLARE MyTaxi : Vehicle
MyTaxi ← T102
```

The names are values of the new type (stored internally as small integers); you cannot assign anything outside the list. Uses: days of the week, colours, status codes.

“State what is meant by an enumerated data type.” *A non-composite user-defined type defined by listing all its possible values (in order).* Because the values are **ordered**, they can be compared and stepped through: with `TYPE Month = (January, February, ..., December)`, the test `IF ThisMonth > June` is legal, and the values are stored internally as integers. The pseudocode has three parts and the exam marks each: the keyword `TYPE`, the identifier with `=`, and the list in brackets separated by commas.

Worked example. Write pseudocode to define an enumerated type for the days on which a school is open (Monday to Friday), and declare a variable of that type set to Wednesday.

```
TYPE SchoolDay = (Monday, Tuesday, Wednesday, Thursday, Friday)
DECLARE Today : SchoolDay
Today ← Wednesday
```

A variable of an enumerated type cannot be given a value outside the list, which is the whole point: `Today ← Saturday` is a compile-time error, whereas a STRING would have accepted "Saturdy".

TYPE Vehicle =



MyTaxi may only hold one of these named values

An enumerated type is a fixed list of named values

Pointer type

A **pointer** 指针 holds the **memory address of another variable** (or NULL for “no target”). Pointers build dynamic structures (linked lists, trees) and pass references without copying.

```
TYPE PNode = ^TNode    // pointer to a TNode
DECLARE p : PNode
p ← NEW TNode
p^.Value ← 42           // dereference to reach the fields
```

To **dereference** 解引用 (`p^`) means to reach the variable it points to.

“State what is meant by a pointer data type.” A non-composite type whose value is the memory address of (a reference to) a variable of a given type. The pseudocode declares the type with a caret before the type it points to, and the exam asks for exactly that line:

```
TYPE SelectParts = ^Parts      // a pointer to a value of type Parts
DECLARE Chosen : SelectParts
Chosen ← ^Keyboard            // Chosen now holds the address of
    ↪ Keyboard
OUTPUT Chosen^                // dereference: the value stored at
    ↪ that address
```

Pointers are what a dynamic **linked list** or **binary tree** (Topic 19) is built from: each node holds a pointer to the next. Two marks are commonly lost here: writing the pointer type as if it held the value itself, and forgetting the caret when reading through the pointer.

a pointer holds an address

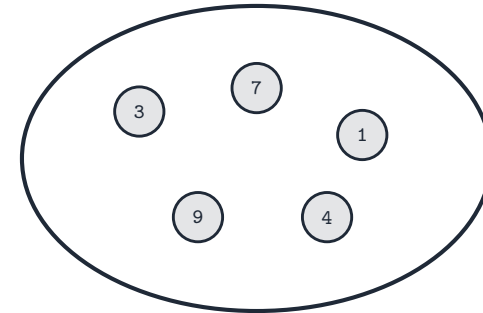


$p^{\wedge}$ dereferences — reach the node’s fields, e.g. $p^{\wedge}.Value$

A pointer holds an address; $p^{\wedge}$ dereferences it to reach the node’s fields

Composite types

A **composite type** 复合类型 (one of the **composite data types**) groups several values under one name.



unordered, every value unique

A set is an unordered collection of unique values

record Student

Name : STRING
Age : INTEGER
Grade : CHAR
Enrolled : BOOLEAN

one name, several fields of different types

A record groups fields of different types under one name

- **record** 记录 (Topic 10) — fields of different types in a `TYPE ... ENDTYPE` block.
- **set** 集合 — an unordered collection of unique values, with operations add, remove, membership test, union, intersection:

```
DECLARE Available : SET OF Colour
Available ← {Red, Blue}
IF Green IN Available THEN ...
```

- **class** 类 / **object** 对象 — the OOP composite type, combining data fields (**at-**

tributes 属性) with operations on them (**methods** 方法). An object is an instance of a class:

```
CLASS Taxi
  PRIVATE Capacity : INTEGER
  PUBLIC FUNCTION GetCapacity() RETURNS INTEGER
    RETURN Capacity
  ENDFUNCTION
ENDCLASS
```

Choosing a type

Use **enumerated** for a value from a fixed list, **pointer** for indirection, **record** for a group of fields, **set** for an unordered unique collection, and **class** when you need state and behaviour together.

“Describe the user-defined data type set” (three marks). *A composite type that holds a collection of values of the same type, in no particular order and with no duplicates; values can be added and removed, and a value can be tested for membership.* Declare the type with SET OF, then define a set constant with its values in brackets:

```
TYPE EvenNumbers = SET OF INTEGER
DEFINE Evens (2, 4, 6, 8, 10, 12) : EvenNumbers
TYPE SymbolSet = SET OF CHAR
DEFINE Operators ('+', '-', '*', '/') : SymbolSet
```

“Describe the user-defined data type record” (three marks). *A composite type made up of a fixed number of fields (items), each with its own identifier and its own type, referred to under a single identifier; the fields are accessed with dot notation.*

Worked example. Write pseudocode to declare a record type **ClubMember** for a club member’s first name, last name, membership code (an integer), date of joining and whether fees have been paid; then declare a variable and set two of its fields.

```
TYPE ClubMember
  DECLARE FirstName : STRING
  DECLARE LastName : STRING
  DECLARE Code : INTEGER
  DECLARE DateJoined : DATE
  DECLARE FeesPaid : BOOLEAN
ENDTYPE

DECLARE NewMember : ClubMember
NewMember.LastName ← "Chen"
NewMember.FeesPaid ← TRUE
```

Every field needs its own **DECLARE** line with an appropriate type, the block ends with **ENDTYPE**, and a **field** 字段 is reached as **variable.field**. Asked to choose a type for each field, match it to the data: a code that is only ever compared is a **STRING** if it can contain letters, an **INTEGER** if arithmetic or ordering is needed; a yes/no is **BOOLEAN**; a date is **DATE**. A field that can take one of a few named values (a pet’s species, a colour) is the one to make an **enumerated** type.

DECLARE Members : ARRAY[1:4] OF ClubMember			
	Code	FeesPaid	LastName
[1]	1042	TRUE	Chen
[2]	1077	FALSE	Li
[3]	1120	TRUE	Okafor
[4]	1183	TRUE	Sato

Members[2].FeesPaid ← TRUE
writes one field of one element

Members[3].LastName
element 3, field LastName

one element = one whole record

An array of records: each element is a whole record, an index chooses the element, and a dot chooses the field

Records in arrays and files. A table of many members is **DECLARE Members : ARRAY[1:100] OF ClubMember**; then **Members[3].LastName** is one field of one element, and a loop over the index processes every record. A record is also the natural unit written to and read from a file (below), one record per **PUTRECORD** or **WRITEFILE**.

Worked example. A composite type **Pet** stores each pet’s name (string), species (one of dog, cat, rabbit or hamster) and weight in kilograms (real). Define the types and declare a variable.

```
TYPE Species = (Dog, Cat, Rabbit, Hamster)
TYPE Pet
  DECLARE Name : STRING
  DECLARE Kind : Species
  DECLARE Weight : REAL
ENDTYPE
DECLARE MyPet : Pet
MyPet.Kind ← Rabbit
```

The enumerated type is defined **first**, because the record uses it: order matters in pseudocode as it does in a compiler.

Classes in pseudocode. A **class** is the composite type that also carries behaviour. The exam asks for the declaration with its attributes marked **PRIVATE**, a **constructor** 构造函数 named **NEW** that sets them, and **PUBLIC** methods to get or change them:

```

CLASS Appointment
    PRIVATE PatientName : STRING
    PRIVATE Treatment : STRING
    PRIVATE Medication : STRING
    PUBLIC PROCEDURE NEW(Name : STRING, Treat : STRING, Med : STRING)
        PatientName ← Name
        Treatment ← Treat
        Medication ← Med
    ENDPROCEDURE
    PUBLIC FUNCTION GetTreatment() RETURNS STRING
        RETURN Treatment
    ENDFUNCTION
ENDCLASS

DECLARE Visit : Appointment
Visit ← NEW Appointment("A. Chen", "filling", "none")
OUTPUT Visit.GetTreatment()

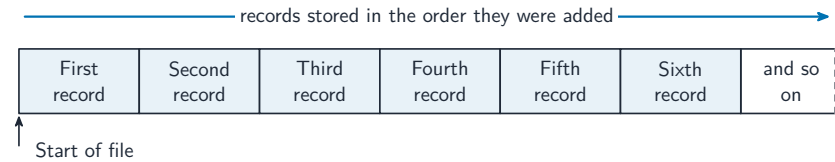
```

Attributes are private so that they can only be changed through methods (encapsulation, Topic 20); the constructor is a procedure called **NEW** with one parameter per attribute; a getter is a function that returns the attribute. Each of these is a separate mark.

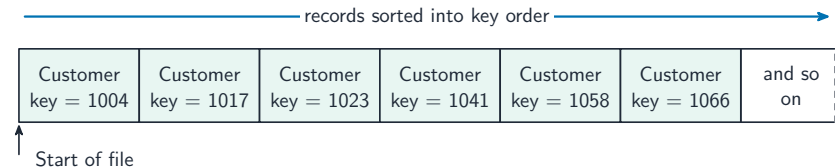
File organisation and access

File organisation 文件组织 is how the data is laid out; **file access** is how the program reaches a record.

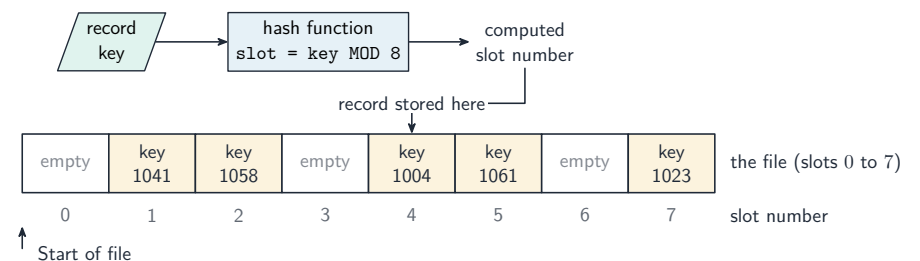
- **serial file** 串行文件 — records in the **order added**, no sorting. Access is sequential only; appending is fast; searching is slow. Used for logs and audit trails.
- **sequential file** 顺序文件 — records **sorted by a key**. Searching is faster (you can stop early or binary-search); inserting is slow (records must shift). Used for master files updated in batch.
- **random file** 随机文件 (direct-access file) — records at positions computed from the key (often by a hash). Direct access by key is very fast; reading in key order is harder. Used for large lookup tables and customer accounts.



Serial file: records are kept in the order they were added



Sequential file: records are sorted by a key field

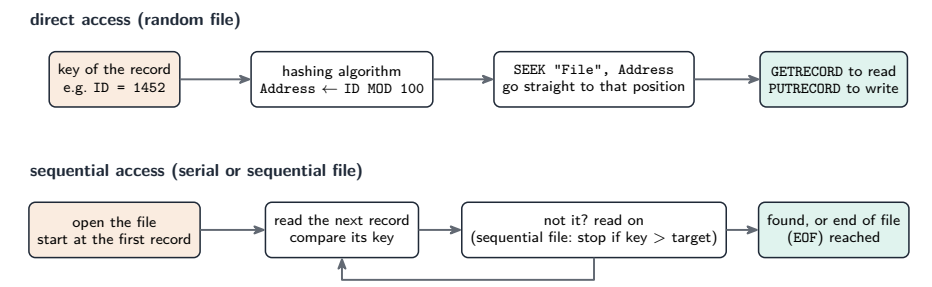


Random file: records sit at positions computed from the key

The two access methods are **sequential access** 顺序存取 (read from start to end) and **direct access** 直接存取 (jump straight to a known position). Match the structure to the dominant operation: single-key lookups favour random; in-order reports favour sequential.

Describing each organisation (the wording that scores). *Serial:* records are stored **one after another in the order in which they were added**, with no ordering by key. *Sequential:* records are stored **in order of a key field** (sorted). *Random:* each record is stored at an **address calculated from its key** by a hashing algorithm, so the records are not in any order. **Comparing serial and sequential:** both store records one after another and both are read sequentially, but a sequential file is ordered by key, so a search can stop as soon as a key larger than the target is

read, and a new record must be inserted in its correct position (usually by rewriting the file), whereas a serial file is simply appended to.



The two access methods as procedures: direct access computes where to look; sequential access looks everywhere in turn

Describing each access method. *Sequential access:* start at the **beginning** of the file and read the records **one after another** (in the order stored) until the required record is found or the end of the file is reached. Applied to a **serial** file this means reading every record up to the match, and reading the whole file to establish that a record is absent; applied to a **sequential** file the search can **stop early**, as soon as a key greater than the target is read. *Direct access:* the **address** of the record is calculated from its key (by a hashing algorithm, or from an index), and the program goes **straight to that position** without reading the records before it; this is the access method for random files, and for a record referenced by a unique address on a disk.

Choosing. A payroll or utility-billing master file processed in batch, every record in turn, suits a **sequential** file; a log of transactions in the order they happened suits a **serial** file; a stock or customer file where single records are looked up and updated by key while the program runs suits a **random** file with direct access.

File handling in pseudocode. The exam expects the standard statements, and Paper 3 sets algorithms that use them:

Task	Statements
open a text file	OPENFILE "Scores.txt" FOR READ (or FOR WRITE, which creates or overwrites, or FOR APPEND)
read or write a line	READFILE "Scores.txt", Line and WRITEFILE "Scores.txt", Line
test for the end	WHILE NOT EOF("Scores.txt")
close	CLOSEFILE "Scores.txt"
open a random file	OPENFILE "Stock.dat" FOR RANDOM
move to a record position	SEEK "Stock.dat", Address
read or write a whole record	GETRECORD "Stock.dat", Item and PUTRECORD "Stock.dat", Item

Worked example. A random file `Stock.dat` holds records of type `StockItem`, stored at the address given by `ItemID MOD 100`. Write pseudocode that stores a new item at its hashed address if that position is empty, reporting the position if it is already in use.

```
DECLARE Item, Existing : StockItem
DECLARE Address : INTEGER
INPUT Item.ItemID, Item.Description, Item.Quantity
Address ← Item.ItemID MOD 100
OPENFILE "Stock.dat" FOR RANDOM
SEEK "Stock.dat", Address
GETRECORD "Stock.dat", Existing
IF Existing.ItemID = 0 THEN           // 0 marks an empty position
    SEEK "Stock.dat", Address
    PUTRECORD "Stock.dat", Item
    OUTPUT "Stored at ", Address
ELSE
    OUTPUT "Position ", Address, " is in use"
ENDIF
CLOSEFILE "Stock.dat"
```

Two details the mark scheme checks: **SEEK before** each `GETRECORD` or `PUTRECORD` (reading moves the position on, so seek again before writing), and the file opened **FOR RANDOM** and closed at the end. To copy every record of a random file to another, loop over the addresses with `SEEK`, `GETRECORD` from one file and `PUTRECORD` to the other, skipping empty positions.

Hashing

A **hash function** 散列函数 (a **hashing algorithm**) takes a record key and produces an **address** where the record is stored. A good one is fast, **deterministic** 确定性,

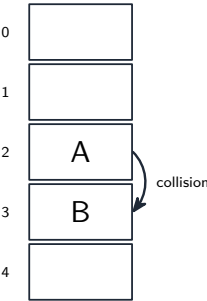
and spreads keys evenly.

Common **hashing algorithms** for N slots: modulo hash $\text{address} \leftarrow \text{key} \bmod N$; folding (split the key, add the pieces, $\bmod N$); a string hash (sum the character codes, $\bmod N$).

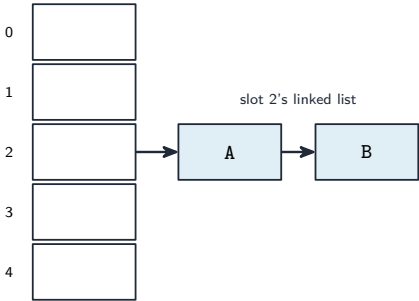
A **collision** 冲突 is when two keys hash to the same address. Three ways to resolve it:

Strategy	How it works	Trade-off
linear probing 线性探测	use the next free slot (wrapping around)	simple, but keys cluster
chaining 链接法	each slot points to a linked list of records	no clustering, but uses more memory
rehashing	apply a second hash function	spreads keys, but more work

linear probing



chaining



Resolving a hash collision: linear probing uses the next free slot; chaining keeps a linked list per slot

To search: hash the key, read that slot; if the keys match you are done, else follow the resolution strategy until a match or an empty slot. To insert: hash the key, write to that slot or the next free one. Keep the **load factor** 装填因子 (records $\div$ slots) below about 70% for near- $O(1)$ lookups.

“Explain what is meant by a hashing algorithm in the context of file access” (three marks). A calculation (function) performed on the key field of a record that produces a value, which is used as the address (location) at which the record is stored in the file and from which it is retrieved. The same calculation on the same key always gives the same address, which is why the record can be found again without searching.

“Outline two methods of overcoming a collision.” (1) **Linear probing** (open addressing): store the record in the **next free** location after the calculated address, wrapping round to the start if necessary; to retrieve, start at the hashed address and read forward until the key matches. (2) An **overflow area** 溢出区 or **chaining**: store the colliding record in a separate overflow area (or a linked list attached to the address), which is searched sequentially after the main address fails to match. Either scores; describe the retrieval as well as the storage.

Worked example. A random file has 11 record positions, numbered 0 to 10, and the hashing algorithm is $\text{Address} \leftarrow \text{Key} \bmod 11$. Records with keys 1250, 1381, 1452, 1613 and 1470 are stored in that order, using linear probing. Show where each record goes, and describe how key 1470 is retrieved.

$1250 \bmod 11 = 7$; $1381 \bmod 11 = 6$; $1452 \bmod 11 = 0$; $1613 \bmod 11 = 7$, a **collision** with 1250, so 1613 takes the next free position, 8; $1470 \bmod 11 = 7$ again, and positions 7 and 8 are full, so 1470 goes to 9. To retrieve 1470: calculate 7, read position 7 (key 1250, no match), read 8 (1613, no), read 9 (1470, found). If an **empty** position is reached before a match, the record is not in the file. Collisions are the price of a small file: a good hashing algorithm spreads the keys evenly, and the file is kept well below full so that probes stay short.

Floating-point numbers

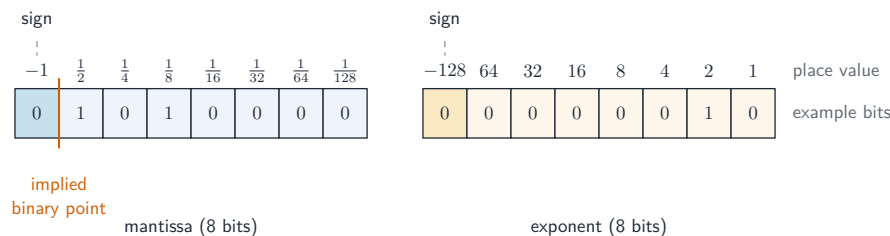
To store **real numbers** of very different sizes, computers use a **floating-point** 浮点 format — a binary form of scientific notation, with two fields:

- a **mantissa** 尾数 — the significant digits.
- an **exponent** 指数 — the power of 2 to multiply by.

Both are stored as **two’s complement** 补码 integers. The value is

$$\text{number} = \text{mantissa} \times 2^{\text{exponent}}.$$

Read the mantissa as a binary fraction — the first bit after the point is worth $1/2$, the next $1/4$, then $1/8$, and so on. So 0.1010000 is $1/2 + 1/8 = 0.625$; with exponent $00000010 (= 2)$ the value is $0.625 \times 2^2 = 2.5$.



The place values of an 8-bit mantissa and an 8-bit exponent

Converting

- binary $\rightarrow$ denary:** read the mantissa (use two's-complement rules if negative) as a fraction, read the exponent as a signed integer, then multiply mantissa by 2^{exponent} .
- denary $\rightarrow$ binary:** write the number as a binary fraction $\times$ a power of 2, then store the mantissa and exponent in the agreed formats.

Worked example. A number has mantissa 10110000 and exponent 00000011. Find its denary value.

The exponent 00000011 is +3. The mantissa begins with a 1, so it is negative. Read as 1.0110000 in two's complement, the sign bit is worth -1 and the fraction bits add $\frac{1}{4} + \frac{1}{8} = 0.375$, so the mantissa is $-1 + 0.375 = -0.625$. Then

$$\text{number} = -0.625 \times 2^3 = -5.0.$$

Worked example. Store +2.5 in this format.

In binary $2.5 = 10.1$. Written as a normalised fraction, $2.5 = 0.101 \times 2^2$. So the mantissa is 01010000 (sign bit 0, then .101) and the exponent is 00000010 (= 2).

The exam's format: two's complement, a mantissa and an exponent

The exam states a format such as **10 bits for the mantissa and 6 bits for the exponent, both in two's complement**. The mantissa's binary point sits after its first (sign) bit, so a positive mantissa is 0.xxxxxxxx and a negative one 1.xxxxxxxx; the exponent is an ordinary signed integer. Every conversion uses the same three moves: read the mantissa as a fraction (two's-complement rules if it starts with 1), read the exponent as an integer, multiply by 2^{exponent} .

Worked example (binary to denary). Mantissa 0101100000, exponent 000011.

Mantissa: $0.101100000_2 = \frac{1}{2} + \frac{1}{8} + \frac{1}{16} = 0.6875$. Exponent: $000011_2 = 3$. Value: $0.6875 \times 2^3 = 5.5$.

Worked example (negative mantissa). Mantissa 1011000000, exponent 000010.

The mantissa starts with 1, so it is negative. Its value is $-1 + 0.011000000_2 = -1 + (\frac{1}{4} + \frac{1}{8}) = -0.625$; exponent = 2; value $-0.625 \times 4 = -2.5$. (Alternatively, take the two's complement of the mantissa, 0101000000 = 0.625, and attach the minus sign.) A **negative exponent** such as 111110 = -2 divides instead: a mantissa of 0.5 with that exponent is $0.5 \times 2^{-2} = 0.125$.

Worked example (denary to binary). Store +6.5 and -6.5 in the 10-bit and 6-bit format, normalised.

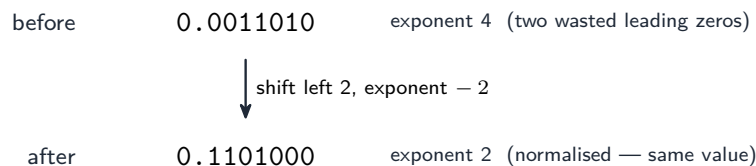
$6.5 = 110.1_2 = 0.1101_2 \times 2^3$, so the mantissa is 0110100000 and the exponent 000011. For -6.5 , take the two's complement of the mantissa: 1001100000 (check: $-1 + 0.0011_2 = -1 + 0.1875 = -0.8125$, and $-0.8125 \times 8 = -6.5$), exponent 000011 unchanged. The sign never goes into the exponent; a negative number has a negative mantissa.

Normalisation

A number is **normalised** 规格化 when the first significant bit is **immediately after the binary point** (no wasted leading zeros). This **maximises precision**, because every mantissa bit carries information. To normalise, shift the mantissa left and decrease the exponent (or shift right and increase it) until the first significant bit is in place; the value is unchanged. For negative (two's-complement) mantissas, the sign bit (1) is followed immediately by a 0.

Recognising and producing normalised form. A positive normalised mantissa begins 01; a negative one begins 10. So 0011000000 is not normalised (shift left one place and subtract one from the exponent: 0110000000, exponent one less) and 1100000000 is not either (shift left until the pattern is 10...). Each shift left of the mantissa must be matched by subtracting one from the exponent, or the value changes.

"Explain why numbers are stored in normalised form" (two marks). (1) It gives the **maximum precision** (accuracy) for the number of bits available, because no bits are wasted on leading zeros (or leading ones for a negative number); (2) each number then has a **unique** representation, so numbers can be compared; and (3) it makes the best use of the available **range**. Any two of these score.



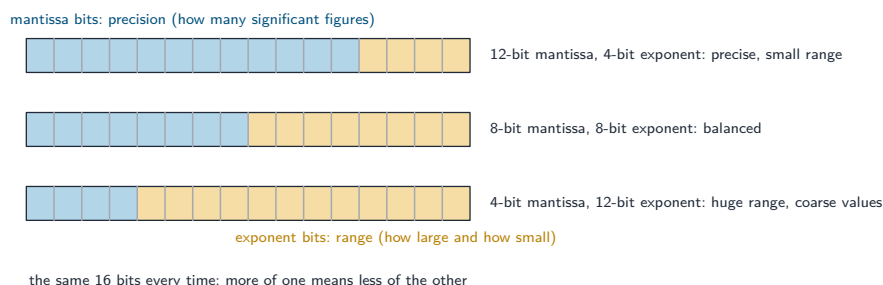
Normalising: shift the mantissa left to remove leading zeros, lowering the exponent by the same amount

Approximation and rounding errors

Many denary reals **cannot be stored exactly** in binary — e.g. 0.1_{10} is the repeating binary fraction $0.000110011\dots_2$, which must be truncated. Consequences:

- **rounding errors** 舍入误差 build up over many operations ($0.1 + 0.2$ is not exactly 0.3).
- **comparisons fail** — test $\text{ABS}(x - 0.3) < 1\text{e-}9$ instead of $x = 0.3$.
- subtracting two nearly-equal values loses precision.
- **overflow** 溢出 (a result too large for the exponent's range) and **underflow** 下溢 (a result too small, rounding to zero) occur when the exponent runs out of range.

For exact needs (currency), use **fixed-point** 定点 or **BCD** 二进制十进数 instead of floating-point.



The same total of bits shared two ways: mantissa bits buy precision, exponent bits buy range, and one can only grow at the other's expense

“Describe the effect of changing the allocation of bits” (three marks). With a fixed total number of bits, **increasing the mantissa** and reducing the exponent gives greater **precision** 精度 (more significant figures, smaller rounding errors) but a smaller **range** 范围 (the largest and smallest magnitudes that can be stored shrink);

increasing the exponent does the opposite: a larger range at the cost of precision. Name both effects and both directions.

Largest and smallest. In the 10-bit mantissa, 6-bit exponent format the largest positive number has mantissa 0111111111 ($= 1 - 2^{-9}$) and exponent 011111 ($= 31$): about 2^{31} . The smallest positive **normalised** number has mantissa 0100000000 ($= 0.5$) and exponent 100000 ($= -32$): $0.5 \times 2^{-32} = 2^{-33}$. The most negative number has mantissa 1000000000 ($= -1$) and exponent 31 : -2^{31} .

“Explain what is meant by overflow and underflow.” **Overflow** occurs when the result of a calculation is **larger than the largest** number that can be represented, so the exponent would need more bits than it has; **underflow** occurs when a result is **smaller than the smallest** (non-zero) number that can be represented, too close to zero for the exponent to express, so it is stored as zero. Both come from the **exponent's** range, not the mantissa's.

Why a binary representation is only an approximation. A binary fraction can only represent sums of $\frac{1}{2}, \frac{1}{4}, \frac{1}{8}, \dots$ exactly; a value such as 0.1 or $\frac{1}{3}$ has an infinite binary expansion, and the mantissa has a fixed number of bits, so the stored value is the nearest one that fits. The difference is a **rounding error**; it is small for one number but **accumulates** over repeated calculations (adding 0.1 ten times may not give exactly 1), which is why real numbers should never be tested for exact equality.

Definitions the examiner accepts

A definition question is marked against fixed wording. Learn these exactly, and give one answer only.

Term	Definition
user-defined data type	a data type defined by the programmer, based on existing types, to represent data specific to the problem
non-composite type	a type defined without reference to another type; it holds a single value (integer, real, enumerated, pointer)
composite type	a type made up of other types; it holds several values under one identifier (record, set, array, class)
enumerated type	a non-composite type defined by listing all its possible values, in order
pointer type	a non-composite type whose value is the memory address of a variable of a given type
set	a composite type holding a collection of values of one type, unordered and without duplicates
record	a composite type with a fixed number of fields, each with its own identifier and type, accessed by dot notation

Term	Definition
class	a composite type combining attributes (data) with the methods (procedures and functions) that act on them; an object is an instance of a class
serial file	records stored one after another in the order in which they were added
sequential file	records stored one after another in order of a key field
random file	records stored at addresses calculated from their keys by a hashing algorithm
sequential access	reading the records in turn from the start of the file until the one required is found
direct access	calculating the address of a record from its key and going straight to that position
hashing algorithm	a calculation on the key of a record that gives the address at which the record is stored and found
collision	two different keys producing the same address
mantissa	the part of a floating-point number that holds its significant bits, as a two's-complement fraction
exponent	the two's-complement integer giving the power of two by which the mantissa is multiplied
normalised	a floating-point number whose mantissa begins 01 (positive) or 10 (negative), so no bits are wasted on leading zeros or ones
overflow	a result too large to be represented in the number of bits available
underflow	a non-zero result too small to be represented, so it is stored as zero
rounding error	the difference between a real number and the nearest value that the binary representation can hold

Exam tips

- Pseudocode declarations are marked line by line: `TYPE ... = (...)` for enumerated, `TYPE ... = ^...` for pointer, `TYPE ... = SET OF ...` then `DEFINE ... (...)` : ... for a set, `TYPE ... DECLARE ... ENDTYPE` for a record, `CLASS ... PRIVATE ... PUBLIC PROCEDURE NEW ... ENDCLASS` for a class.
- Match the type to the data: fixed named values, enumerated; a group of different fields, record; a collection of unique values, set; data plus behaviour, class; an address, pointer.
- File organisation is how records are **stored**; file access is how they are **found**. Serial and sequential are read sequentially; random files use direct access via a

hash of the key. Sequential search of a **sequential** file can stop early; of a serial file it cannot.

- Random-file pseudocode: `OPENFILE ... FOR RANDOM, SEEK` before every `GETRECORD` or `PUTRECORD`, `CLOSEFILE` at the end. Say how a collision is resolved when you describe hashing.
- Floating point: mantissa as a two's-complement fraction (point after the sign bit), exponent as an integer, multiply by 2^{exponent} ; shift left and subtract one from the exponent to normalise; the mantissa buys precision, the exponent buys range.
- The three "explain" stock answers: why normalise (precision, unique form, range), the effect of re-allocating bits (precision against range), and why 0.1 cannot be stored exactly (an infinite binary fraction in a finite mantissa).

Common mistakes

- Writing `DECLARE` instead of `TYPE` for a new type, or leaving out `ENDTYPE`; declaring a set without `SET OF`, or an enumerated type with quotation marks round its values.
- Putting the sign of a floating-point number in the exponent; the sign is the first bit of the mantissa.
- Reading a negative mantissa as if it were sign-and-magnitude; it is two's complement, so 1011000000 is -0.625 , not -0.375 .
- Shifting the mantissa to normalise without changing the exponent, or changing it the wrong way (shift left, exponent down).
- Describing a random file as "in random order"; the records are at addresses computed from their keys.
- Saying sequential access reads "the whole file" for a sequential file; it stops when a larger key is met.
- Explaining hashing without saying what the calculated value is used for (the address to store and retrieve the record), or without a way of handling collisions.
- Defining overflow as "too many digits" instead of a result beyond the largest representable value, or blaming the mantissa for it.