

2024



# AP<sup>®</sup> Physics C: Mechanics

## Free-Response Questions Set 2

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AP<sup>®</sup> Physics C: Mechanics 2024 Free-Response Questions

### ADVANCED PLACEMENT PHYSICS C TABLE OF INFORMATION

| CONSTANTS AND CONVERSION FACTORS                                                                                    |                                                                                                    |
|---------------------------------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------|
| Proton mass, $m_p = 1.67 \times 10^{-27}$ kg                                                                        | Electron charge magnitude, $e = 1.60 \times 10^{-19}$ C                                            |
| Neutron mass, $m_n = 1.67 \times 10^{-27}$ kg                                                                       | 1 electron volt, $1 \text{ eV} = 1.60 \times 10^{-19}$ J                                           |
| Electron mass, $m_e = 9.11 \times 10^{-31}$ kg                                                                      | Speed of light, $c = 3.00 \times 10^8$ m/s                                                         |
| Avogadro's number, $N_0 = 6.02 \times 10^{23}$ mol <sup>-1</sup>                                                    | Universal gravitational constant, $G = 6.67 \times 10^{-11} (\text{N}\cdot\text{m}^2)/\text{kg}^2$ |
| Universal gas constant, $R = 8.31 \text{ J}/(\text{mol}\cdot\text{K})$                                              | Acceleration due to gravity at Earth's surface, $g = 9.8 \text{ m/s}^2$                            |
| Boltzmann's constant, $k_B = 1.38 \times 10^{-23} \text{ J/K}$                                                      |                                                                                                    |
| 1 unified atomic mass unit, $1 \text{ u} = 1.66 \times 10^{-27} \text{ kg} = 931 \text{ MeV}/c^2$                   |                                                                                                    |
| Planck's constant, $h = 6.63 \times 10^{-34} \text{ J}\cdot\text{s} = 4.14 \times 10^{-15} \text{ eV}\cdot\text{s}$ |                                                                                                    |
|                                                                                                                     | $hc = 1.99 \times 10^{-25} \text{ J}\cdot\text{m} = 1.24 \times 10^3 \text{ eV}\cdot\text{nm}$     |
| Vacuum permittivity, $\epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2/(\text{N}\cdot\text{m}^2)$                      |                                                                                                    |
| Coulomb's law constant, $k = 1/(4\pi\epsilon_0) = 9.0 \times 10^9 (\text{N}\cdot\text{m}^2)/\text{C}^2$             |                                                                                                    |
| Vacuum permeability, $\mu_0 = 4\pi \times 10^{-7} (\text{T}\cdot\text{m})/\text{A}$                                 |                                                                                                    |
| Magnetic constant, $k' = \mu_0/(4\pi) = 1 \times 10^{-7} (\text{T}\cdot\text{m})/\text{A}$                          |                                                                                                    |
| 1 atmosphere pressure, $1 \text{ atm} = 1.0 \times 10^5 \text{ N/m}^2 = 1.0 \times 10^5 \text{ Pa}$                 |                                                                                                    |

| UNIT<br>SYMBOLS | meter, m     | mole, mol  | watt, W       | farad, F           |
|-----------------|--------------|------------|---------------|--------------------|
|                 | kilogram, kg | hertz, Hz  | coulomb, C    | tesla, T           |
|                 | second, s    | newton, N  | volt, V       | degree Celsius, °C |
|                 | ampere, A    | pascal, Pa | ohm, $\Omega$ | electron volt, eV  |
|                 | kelvin, K    | joule, J   | henry, H      |                    |

| PREFIXES   |        |        |
|------------|--------|--------|
| Factor     | Prefix | Symbol |
| $10^9$     | giga   | G      |
| $10^6$     | mega   | M      |
| $10^3$     | kilo   | k      |
| $10^{-2}$  | centi  | c      |
| $10^{-3}$  | milli  | m      |
| $10^{-6}$  | micro  | $\mu$  |
| $10^{-9}$  | nano   | n      |
| $10^{-12}$ | pico   | p      |

| VALUES OF TRIGONOMETRIC FUNCTIONS FOR COMMON ANGLES |    |              |     |              |     |              |          |
|-----------------------------------------------------|----|--------------|-----|--------------|-----|--------------|----------|
| $\theta$                                            | 0° | 30°          | 37° | 45°          | 53° | 60°          | 90°      |
| $\sin \theta$                                       | 0  | 1/2          | 3/5 | $\sqrt{2}/2$ | 4/5 | $\sqrt{3}/2$ | 1        |
| $\cos \theta$                                       | 1  | $\sqrt{3}/2$ | 4/5 | $\sqrt{2}/2$ | 3/5 | 1/2          | 0        |
| $\tan \theta$                                       | 0  | $\sqrt{3}/3$ | 3/4 | 1            | 4/3 | $\sqrt{3}$   | $\infty$ |

- The following assumptions are used in this exam.
- The frame of reference of any problem is inertial unless otherwise stated.
  - The direction of current is the direction in which positive charges would drift.
  - The electric potential is zero at an infinite distance from an isolated point charge.
  - All batteries and meters are ideal unless otherwise stated.
  - Edge effects for the electric field of a parallel plate capacitor are negligible unless otherwise stated.

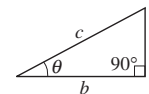
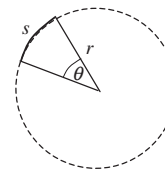
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## ADVANCED PLACEMENT PHYSICS C EQUATIONS

| MECHANICS                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              | ELECTRICITY AND MAGNETISM                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   |
|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| $v_x = v_{x0} + a_x t$<br>$x = x_0 + v_{x0} t + \frac{1}{2} a_x t^2$<br>$v_x^2 = v_{x0}^2 + 2a_x(x - x_0)$<br>$\vec{a} = \frac{\sum \vec{F}}{m} = \frac{\vec{F}_{net}}{m}$<br>$\vec{F} = \frac{d\vec{p}}{dt}$<br>$\vec{J} = \int \vec{F} dt = \Delta \vec{p}$<br>$\vec{p} = m\vec{v}$<br>$ \vec{F}_f  \leq \mu  \vec{F}_N $<br>$\Delta E = W = \int \vec{F} \cdot d\vec{r}$<br>$K = \frac{1}{2} m v^2$<br>$P = \frac{dE}{dt}$<br>$P = \vec{F} \cdot \vec{v}$<br>$\Delta U_g = mg\Delta h$<br>$a_c = \frac{v^2}{r} = \omega^2 r$<br>$\vec{\tau} = \vec{r} \times \vec{F}$<br>$\vec{\alpha} = \frac{\sum \vec{\tau}}{I} = \frac{\vec{\tau}_{net}}{I}$<br>$I = \int r^2 dm = \sum mr^2$<br>$x_{cm} = \frac{\sum m_i x_i}{\sum m_i}$<br>$v = r\omega$<br>$\vec{L} = \vec{r} \times \vec{p} = I\vec{\omega}$<br>$K = \frac{1}{2} I \omega^2$<br>$\omega = \omega_0 + \alpha t$<br>$\theta = \theta_0 + \omega_0 t + \frac{1}{2} \alpha t^2$ | $ \vec{F}_E  = \frac{1}{4\pi\epsilon_0} \left  \frac{q_1 q_2}{r^2} \right $<br>$\vec{E} = \frac{\vec{F}_E}{q}$<br>$\oint \vec{E} \cdot d\vec{A} = \frac{Q}{\epsilon_0}$<br>$E_x = -\frac{dV}{dx}$<br>$\Delta V = -\int \vec{E} \cdot d\vec{r}$<br>$V = \frac{1}{4\pi\epsilon_0} \sum_i \frac{q_i}{r_i}$<br>$U_E = qV = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r}$<br>$\Delta V = \frac{Q}{C}$<br>$C = \frac{\kappa \epsilon_0 A}{d}$<br>$C_p = \sum_i C_i$<br>$\frac{1}{C_s} = \sum_i \frac{1}{C_i}$<br>$I = \frac{dQ}{dt}$<br>$U_C = \frac{1}{2} Q \Delta V = \frac{1}{2} C (\Delta V)^2$<br>$R = \frac{\rho \ell}{A}$<br>$\vec{E} = \rho \vec{J}$<br>$I = Nev_d A$<br>$I = \frac{\Delta V}{R}$<br>$R_s = \sum_i R_i$<br>$\frac{1}{R_p} = \sum_i \frac{1}{R_i}$<br>$P = I \Delta V$<br>$A = \text{area}$<br>$B = \text{magnetic field}$<br>$C = \text{capacitance}$<br>$d = \text{distance}$<br>$E = \text{electric field}$<br>$\mathcal{E} = \text{emf}$<br>$F = \text{force}$<br>$I = \text{current}$<br>$J = \text{current density}$<br>$L = \text{inductance}$<br>$\ell = \text{length}$<br>$n = \text{number of loops of wire per unit length}$<br>$N = \text{number of charge carriers per unit volume}$<br>$P = \text{power}$<br>$Q = \text{charge}$<br>$q = \text{point charge}$<br>$R = \text{resistance}$<br>$r = \text{radius or distance}$<br>$t = \text{time}$<br>$U = \text{potential or stored energy}$<br>$V = \text{electric potential}$<br>$v = \text{velocity or speed}$<br>$\rho = \text{resistivity}$<br>$\Phi = \text{flux}$<br>$\kappa = \text{dielectric constant}$<br>$\vec{F}_M = q\vec{v} \times \vec{B}$<br>$\oint \vec{B} \cdot d\vec{\ell} = \mu_0 I$<br>$d\vec{B} = \frac{\mu_0}{4\pi} \frac{I d\vec{\ell} \times \hat{r}}{r^2}$<br>$\vec{F} = \int I d\vec{\ell} \times \vec{B}$<br>$B_s = \mu_0 n I$<br>$\Phi_B = \int \vec{B} \cdot d\vec{A}$<br>$\mathcal{E} = \oint \vec{E} \cdot d\vec{\ell} = -\frac{d\Phi_B}{dt}$<br>$\mathcal{E} = -L \frac{dI}{dt}$<br>$U_L = \frac{1}{2} L I^2$ |

## ADVANCED PLACEMENT PHYSICS C EQUATIONS

| GEOMETRY AND TRIGONOMETRY                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       | CALCULUS                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           |
|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <p>Rectangle<br/> <math>A = bh</math></p> <p>Triangle<br/> <math>A = \frac{1}{2} bh</math></p> <p>Circle<br/> <math>A = \pi r^2</math><br/> <math>C = 2\pi r</math><br/> <math>s = r\theta</math></p> <p>Rectangular Solid<br/> <math>V = \ell wh</math></p> <p>Cylinder<br/> <math>V = \pi r^2 \ell</math><br/> <math>S = 2\pi r \ell + 2\pi r^2</math></p> <p>Sphere<br/> <math>V = \frac{4}{3} \pi r^3</math><br/> <math>S = 4\pi r^2</math></p> <p>Right Triangle<br/> <math>a^2 + b^2 = c^2</math><br/> <math>\sin \theta = \frac{a}{c}</math><br/> <math>\cos \theta = \frac{b}{c}</math><br/> <math>\tan \theta = \frac{a}{b}</math></p> | <p><math>A = \text{area}</math><br/> <math>C = \text{circumference}</math><br/> <math>V = \text{volume}</math><br/> <math>S = \text{surface area}</math><br/> <math>b = \text{base}</math><br/> <math>h = \text{height}</math><br/> <math>\ell = \text{length}</math><br/> <math>w = \text{width}</math><br/> <math>r = \text{radius}</math><br/> <math>s = \text{arc length}</math><br/> <math>\theta = \text{angle}</math></p> <p><math>\frac{df}{dx} = \frac{df}{du} \frac{du}{dx}</math><br/> <math>\frac{d}{dx}(x^n) = nx^{n-1}</math><br/> <math>\frac{d}{dx}(e^{ax}) = ae^{ax}</math><br/> <math>\frac{d}{dx}(\ln ax) = \frac{1}{x}</math><br/> <math>\frac{d}{dx}[\sin(ax)] = a \cos(ax)</math><br/> <math>\frac{d}{dx}[\cos(ax)] = -a \sin(ax)</math><br/> <math>\int x^n dx = \frac{1}{n+1} x^{n+1}, n \neq -1</math><br/> <math>\int e^{ax} dx = \frac{1}{a} e^{ax}</math><br/> <math>\int \frac{dx}{x+a} = \ln x+a </math><br/> <math>\int \cos(ax) dx = \frac{1}{a} \sin(ax)</math><br/> <math>\int \sin(ax) dx = -\frac{1}{a} \cos(ax)</math></p> <p><b>VECTOR PRODUCTS</b><br/> <math>\vec{A} \cdot \vec{B} = AB \cos \theta</math><br/> <math> \vec{A} \times \vec{B}  = AB \sin \theta</math></p> |



Begin your response to **QUESTION 1** on this page.

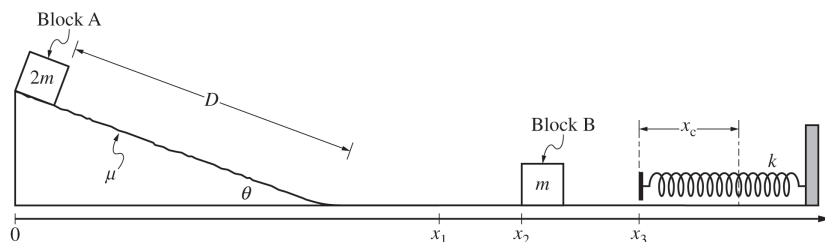
**PHYSICS C: MECHANICS**

**SECTION II**

**Time—45 minutes**

**3 Questions**

**Directions:** Answer all three questions. The suggested time is about 15 minutes for answering each of the questions, which are worth 15 points each. The parts within a question may not have equal weight. Show all your work in this booklet in the spaces provided after each part.



Note: Figure not drawn to scale.

1. Blocks A and B of masses  $2m$  and  $m$ , respectively, are arranged in a setup consisting of a ramp that makes an angle  $\theta$  with a smooth horizontal table and an ideal spring of spring constant  $k$  fixed to a wall, as shown. Block A is held at rest a distance  $D$  up the ramp, and Block B is at rest on the horizontal table. The coefficient of kinetic friction between Block A and the rough ramp is  $\mu$  in the region of length  $D$ , and there is negligible friction between the blocks and the smooth table.

**GO ON TO THE NEXT PAGE.**

Continue your response to **QUESTION 1** on this page.

At time  $t = 0$ , Block A is located at horizontal position  $x = 0$  and is released from rest. After the block is released, the following occurs.

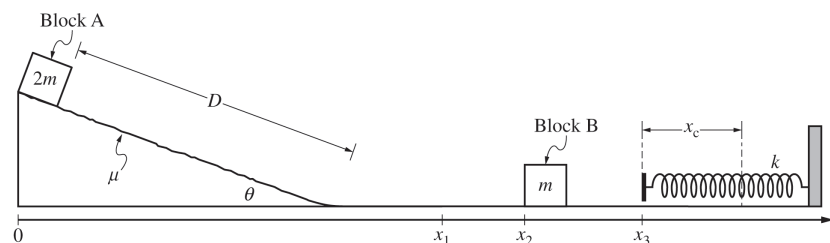
- At time  $t = t_1$ , Block A has traveled a distance  $D$  down the ramp, has transitioned to the table, and is moving with speed  $v$  at  $x = x_1$ .
- At time  $t = t_2$ , Block A is at  $x = x_2$  when it collides with and sticks to Block B.
- At time  $t = t_3$ , the combined blocks A and B are at  $x = x_3$  when they collide with and stick to the spring in its equilibrium position.
- At time  $t = t_4$ , the combined blocks A and B are instantaneously at rest and the spring is compressed a distance  $x_c$  from its equilibrium position.

(a) For parts (a)(i) and (a)(ii), express your answer in terms of  $m$ ,  $\theta$ ,  $D$ ,  $\mu$ ,  $x_c$ , and physical constants, as appropriate.

i. **Derive** an expression for the speed  $v$  of Block A at time  $t_1$ .

ii. **Derive** an expression for the spring constant  $k$  of the spring.

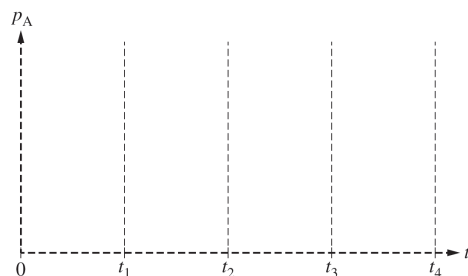
**GO ON TO THE NEXT PAGE.**

Continue your response to **QUESTION 1** on this page.

Note: Figure not drawn to scale.

(b)

- i. On the following axes, **sketch** a graph of the magnitude of the momentum  $p_A$  of Block A as a function of time  $t$  from  $t = 0$  to  $t_4$ .



- ii. Use principles of forces to **justify** the graph drawn in part (b)(i) for the time interval  $t = t_3$  to  $t = t_4$ . Explicitly reference features of the shape of the graph you drew in part (b)(i).

**GO ON TO THE NEXT PAGE.**Continue your response to **QUESTION 1** on this page.

For times  $t > t_4$ , the two-block-spring system oscillates with period  $T_O$ . The procedure is then repeated using a new ramp, where there is negligible friction between Block A and the ramp.

- (c) **Indicate** how the new period of oscillation  $T_N$  in the procedure that uses the new ramp compares with the period of oscillation  $T_O$  from the original procedure.

\_\_\_\_\_  $T_N > T_O$       \_\_\_\_\_  $T_N < T_O$       \_\_\_\_\_  $T_N = T_O$

Briefly **justify** your answer.

**GO ON TO THE NEXT PAGE.**

Begin your response to **QUESTION 2** on this page.

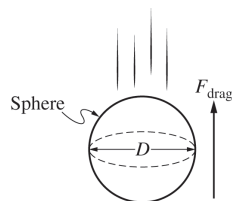


Figure 1

2. A student drops a sphere of mass  $m$  from rest. The air exerts a drag force of magnitude  $F_{\text{drag}}$  on the sphere, as shown in Figure 1. The student models the magnitude of the drag force as  $F_{\text{drag}} = bv$ , where  $v$  is the speed of the sphere and  $b$  is a positive constant with appropriate units.

(a) **Derive**, but do NOT solve, a differential equation that could be used to determine the speed  $v$  of the sphere as a function of time  $t$ . Express your answer in terms of given quantities and physical constants, as appropriate.

GO ON TO THE NEXT PAGE.

Continue your response to **QUESTION 2** on this page.

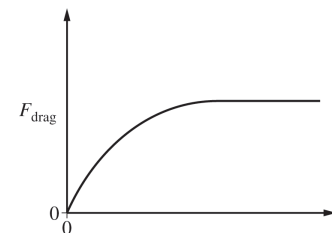


Figure 2

- (b) The student sketches the drag force  $F_{\text{drag}}$  exerted on the sphere as a function of time  $t$ , as shown in Figure 2.

i. **Draw** a vertical line on the sketch in Figure 2 to indicate the earliest time at which  $F_{\text{drag}}$  is equal to the magnitude of the weight of the sphere, which occurs when the sphere reaches terminal speed. Label this time as  $t_T$  on the time axis.

ii. **Justify** the location of  $t_T$ . Explicitly reference appropriate features of the sketch in Figure 2.

- (c) Suppose the student throws the same sphere downward with a nonzero initial speed. The magnitude of the new drag force at terminal speed after being thrown downward is  $F_{\text{new}}$ .

**Indicate** whether  $F_{\text{new}}$  would be greater than, less than, or equal to the magnitude of  $F_{\text{drag}}$  at terminal speed represented in Figure 2.

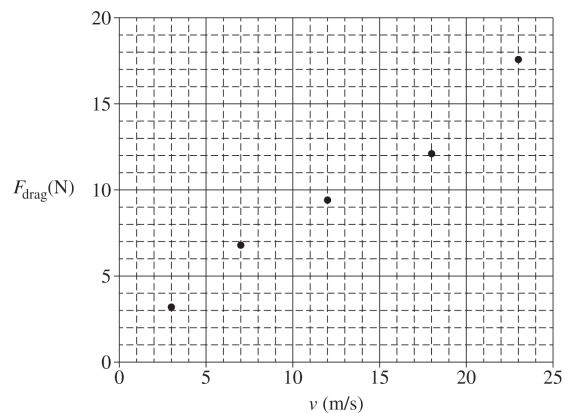
\_\_\_\_\_ Greater than      \_\_\_\_\_ Less than      \_\_\_\_\_ Equal to

Briefly **justify** your answer.

GO ON TO THE NEXT PAGE.

Continue your response to **QUESTION 2** on this page.

- (d) The student conducts an experiment to better understand the relationship between  $F_{\text{drag}}$  and  $v$ . The student makes measurements to calculate and graph the magnitude of  $F_{\text{drag}}$  as a function of  $v$  for the falling sphere.



- Draw the best-fit line for the data.
- Use the best-fit line to **calculate** an experimental value for  $b$ .

GO ON TO THE NEXT PAGE.

Continue your response to **QUESTION 2** on this page.

A student claims that the terminal speed  $v_T$  of the sphere depends on the diameter  $D$  of the sphere. The student designs an experiment to collect data that can be used to provide evidence to support the claim.

- (e) The student has access to but does not have to use all of the following equipment.

- Sphere Set 1: spheres of the same known mass with different known diameters
- Sphere Set 2: spheres of the same known diameter with different known masses
- A motion detector that can measure velocity as a function of time
  - Indicate** two quantities that when graphed could be used to determine whether the diameter of the sphere affects the terminal speed.

Vertical axis: \_\_\_\_\_ Horizontal axis: \_\_\_\_\_

- Briefly **describe** how the quantities graphed could be used to determine the relationship between sphere diameter and terminal speed.

GO ON TO THE NEXT PAGE.

Begin your response to **QUESTION 3** on this page.

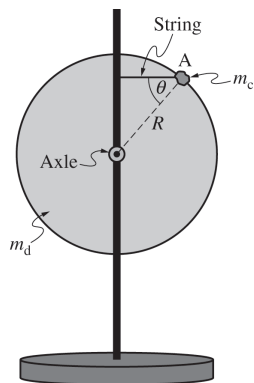
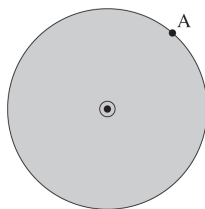


Figure 1

Note: Figure not drawn to scale.

3. A uniform disk of radius  $R$  and mass  $m_d$  is attached to a vertical pole by a horizontal axle that passes through the center of the disk. Friction between the axle and the disk is negligible. A lump of clay of mass  $m_c$  is attached to the edge of the disk at Point A. The size of the lump of clay is small compared with the radius of the disk. A horizontal string is connected from the pole to the edge of the disk at Point A. The string makes an angle  $\theta$  with the line between Point A and the axle, as shown in Figure 1.

- (a) On the following representation of the clay-disk system, **draw** and **label** the external forces (not components) exerted on the system. Each force must be represented by a distinct arrow that starts on, and points away from, the point at which the force is exerted on the system.



**GO ON TO THE NEXT PAGE.**

Continue your response to **QUESTION 3** on this page.

- (b) **Derive** an expression for the tension  $F_T$  in the string when the clay is at Point A, as shown in Figure 1, in terms of  $R$ ,  $m_d$ ,  $m_c$ ,  $\theta$ , and physical constants, as appropriate.

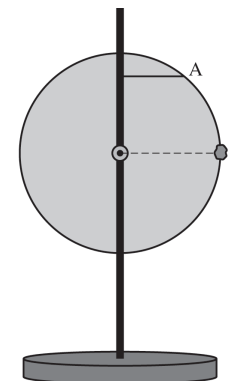


Figure 2

Note: Figure not drawn to scale.

- (c) The string remains connected to the edge of the disk at Point A. The clay is moved to Point B, which is horizontally in line with the axle, as shown in Figure 2. How does the new tension  $F_{T, \text{new}}$  compare with tension  $F_T$  from part (b)? **Justify** your reasoning.

**GO ON TO THE NEXT PAGE.**

Continue your response to **QUESTION 3** on this page.

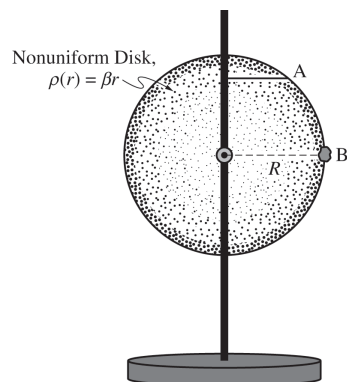


Figure 3

Note: Figure not drawn to scale.

(d) A nonuniform disk is now attached to the axle. The lump of clay is attached to the disk at Point B, as shown in Figure 3. The clay has mass  $m_c = 0.60$  kg and the disk has a radius  $R = 0.30$  m. The mass density of the disk varies radially and can be modeled by  $\rho(r) = \beta r$ , where  $r$  is the radial distance from the axle and  $\beta = 4.0$  kg/m<sup>3</sup>.

i. **Calculate** the rotational inertia of the disk about the axle.

ii. The string connecting the disk to the pole is cut. **Calculate** the magnitude of the initial angular acceleration of the clay-disk system.

**GO ON TO THE NEXT PAGE.**

**STOP**

**END OF EXAM**